Work Program for B2FMaths@Home

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## How to use this work program

## Accessing the online resources

To access the online resources, please go to: https://www.backtofrontmaths.com.au/b2fmathshome

## Running the program each week

Each week is designed with five maths lessons so that you can do it each day. Different days have different types of lessons to make sure that students experience the kind of thinking that they need to continue growing in maths. The types of lessons include:

- At-home investigation: This is a hands-on task where students explore a new idea before they are taught that skill. They need to come up with an idea to try to solve the problem, try out their idea, decide if it worked or not, try again if needed, and explain what they did. If your child has time with your teacher with a webcam, the teacher will generally be doing this lesson with your child. This is the lesson that will require the heaviest input from you to help your child think through an idea and generally requires the use of some hands-on materials that are listed in the information page.
- Connecting lesson: This type of lesson has questions that lead students to develop their ideas and learn a new skill. It should be fairly easy for a student to do, but you will need to be available to read the question to your child as needed, encourage them to think further, and make sure that they complete the work. Most of these lessons will include 10 minutes of practising number operations or concepts through activities or games.
- Interleaved practise lesson: This type of lesson provides 8-10 questions from different areas of maths so that students practise remembering what they have previously been taught. Some of the questions may not be easy for your child, so feel free to help whenever you see them struggling.
- Generalising lesson: This lesson contains some extension material for use if your child found the week's lessons too easy. If you would prefer, you can spend this lesson playing more of the number games that are included in the connecting lesson or giving your child time to complete any of the lessons that they have not yet done.


## Getting help

The website above will have answers to frequently asked questions as well as videos to help you successfully teach your child at home. If you have further questions or need support, please contact your child's teacher directly using the contact details that they have provided to you. If they can't answer your questions, they will contact the B2FMaths@Home team directly to get an answer within 3 days.

## What you need to know this week

## Week overview

This week we are teaching the concept arrays and counting patterns. We will particularly be focusing on arrays of objects arranged into a grid-like pattern (e.g. tiles or the top of Lego blocks). This model for multiplication and division has links with many other concepts in later years, such as area, volume, fractions and helps develop a firm foundation for understanding algebra.

## Students need to understand:

- Distributive Property: Arrays can be easily split to make multiplying large numbers easier.



## 4 sevens is the same as

## 4 fives and 4 twos

$$
4 \times 7=4 \times 5+4 \times 2
$$

- Commutative Property: Arrays can be rotated to demonstrate that $4 \times 3=3 \times 4$.



## 4 threes $=3$ fours

- Factors are the length and the width of an array. The multiple is the amount altogether.
- Prime numbers, like 7, can only be made by multiplying 1 by itself. That means that they only have 2 factors: themselves and 1. When we arrange prime numbers into arrays, they make lines.

- Composite numbers have more than 2 factors. They make arrays other than in one line.
- Even numbers can all make arrays with 2 on one side (as one factor). Odd numbers can't.
- Square numbers can make square arrays.



## Structural stages

Here are some drawings to show what to look out for if you are worried about your child. We want children to be in the "structural" stage at this point, rather than one of the earlier phases. Please contact your child's teacher if you are concerned.

Look at your child's drawings to determine what structural level they are at. Emphasise moving to the next structural stage rather than drawing larger amounts. For teachers: Joanne Mulligan has more information on developing structural thinking in the PASMAP research available online.

Each of the drawings below is of a tens frame (rectangle with 2 rows of 5 ), drawn by a child who is familiar with tens frames but can't see one. Each drawing was completed by a child aged between 5 and 8 .

Emergent: correct number of rows or columns, but not both, or just 10 in one line but without 2 rows


Partial structural: can draw 10, but not also keep the structure of rows and columns, often this means 2 rows of 5 but not having the squares touching


Structural: both drawings show structural thinking, however the dots on the images show that the child needed to check that there really were 10


## Monday: At-Home Investigation

## You will need:

- Grid paper that is provided (you will need multiple copies)
- Coloured pencils


## Steps:

1. Make sure you have read "What you need to know this week" so that you know what to emphasise with your child.
2. Read the sheet to your child. Encourage your child to come up with many different rectangles or arrays using 60 squares (e.g. $6 \times 10,15 \times 4$ )
3. Discuss what your child found out with them. Keep in mind the ideas from the "What you need to know this week" section so that you can ask questions that are appropriate to the issues identified. Try to encourage your child to explain how they have solved the problem.
4. 100 is another number with lots of factors. That is because it also has 4 prime factors $(2,2,5,5)$. Others include $54(3,3,3,2), 64(2,2,2,2,2,2), 96(2,2,2,2,2,3)$ and $90(3,3,2,5)$. To find them, simply try multiplying lots of small prime numbers together, then seeing what combinations you can come up with. Having different combinations of numbers gives more interesting factors.

## Extension:

What if you had to build rectangular prisms with 60 blocks rather than just drawing flat rectangles? How many unique 3D shapes could you build (if you turn the shape side ways then it still counts as the same shape)?

## Please note:

By the end of year 4, your child was expected to recall all single digit multiplication facts (up to $10 \times 10$ ). Now is a great time to practise these with your child so that their previous knowledge is not lost, or to build greater recall if they have not yet mastered basic facts.

## At-Home Investigation

How many different arrays can we make with 60 squares or blocks?

## Draw the arrays and label them

Use the grid paper to draw as many unique arrays using 60 squares as you can. In this activity, $6 \times 10$ is considered to be the same as $10 \times 6$, so you only need to draw it once. You will probably need multiple sheets of grid paper and will also need to cut it and stick it together to make the right sizes.

For each array, label the factors (the sides). Write each set of factors here:

## Think it through

Can you find 2 other numbers between 50 and 100 that have as many or more factors than 60 ?
Write the numbers and sketch the arrays and list the factors here:

## Apply your thinking:

The factors of 60 can be broken down further into prime factors using a factor tree. The more prime factors a number has, the more factors it will have in general. Look at the factor tree below for 60. Use the same thinking to make a prime factor tree for the numbers you looked at for the previous question.

What happens if you multiply the prime factors in a different order? Can you change the result? What do you find?


This is called the Commutative Property of multiplication and has important links to algebra.


## Tuesday: Connecting Lesson

## Number task for 10-15 minutes: Finding multiples

Roll a dice 4 times to get 4 numbers, or just pick any 4 numbers between 1 and 8 .

1. List all the different multiples can you make using any 2 of the 4 numbers.
2. What would you get if you multiply all 4 numbers?
3. Which of the numbers are prime, which are composite?

Alternative: complete one of the multiplication grids on the following page.

## Worksheet task: 20-30 minutes

This lesson provides an opportunity for your child to extend their knowledge of multiplication by tens and ones to include multiplying 2-digit numbers together. There is a diagram showing the array which should be helpful. This diagram makes use of the distributive property which is explained in the introduction. Please give your child just the first sheet rather than providing all three at once. Use the second sheet only once they have had a try thinking about a model. The third sheet provides an explanation and some practice questions.

This lesson should mostly be a review for students in year 7. The important part is the visual model, which creates a direct link to algebra. Understanding that the distributive property also applies to algebra is an important part of achieving the "C" standard at Year 7.

Multiplication practice grids:

|  | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 2 |  |  |  |  |  |  |  |  |  |
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|  | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
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|  | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
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|  | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
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| 8 |  |  |  |  |  |  |  |  |  |
| 9 |  |  |  |  |  |  |  |  |  |
| 10 |  |  |  |  |  |  |  |  |  |

## Multiplying two-digit numbers

Use your previous knowledge of multiplication to help you to solve the following problems.

What we already know how to do:
34
X $\qquad$ ones

Sketch what this looks like, and break your array into the tens and ones parts. You do not need to show every single square, just make the rectangle into roughly the right proportions.

What about if we were multiplying by tens instead of ones?


What would it look like to multiply 34 by three tens and also by three ones ( $\mathbf{3 4} \times \mathbf{3 3}$ )?
Use the space below to sketch this very simply and work it out:

Here is an array for $24 \times 23$. Use the parts to see if you can work out what the answer is.


Work out how many squares there are in each different part of the diagram above. Do you need to count every square or is there an easy way to work out how many there are? Use the space below to show your calculations for each part of the array, then work out how many squares there are altogether.

Using a simplified array or written strategies is faster than drawing all of the boxes in an array. Look at the simplified array below and the written strategy. See if you can work out how they are related. Draw lines between the parts in the written strategy that relate to the array.


Written Strategy:
$\begin{array}{r}24 \\ \times \quad 23 \\ \hline 12\end{array}$
60
80
400
552

Explain how the written strategy works using your own words:

Try solving the questions below. Check that you are right by sketching a simplified array.

| 35 |  | 28 |
| ---: | ---: | ---: | ---: | ---: |
| $x$ | $x$ | 35 |
| 23 | $x$ | 21 |

$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

## Wednesday: Connecting Lesson

This lesson asks your child to connect what they have learned over the past two days to work out the pattern for multiplying with decimal numbers. Feel free to provide a calculator for your child (including a calculator app on a phone) to take the pain out of the calculation side and focus instead on the patterns.

## Number game for 10-15 minutes: Array fun

You will need: a print out of the grid from Monday, 2 colours of pencil, one or two dice.

1. Player one rolls the two dice (or one dice two times). The numbers rolled are the length and width of your array to colour! (e.g. a 4 and a 3 would need a $4 \times 3$ array) You can turn it sideways to fit. Colour your array on the grid, then it is the other player's turn.
2. The player who wins is the last player who can draw their array.

Alternative: complete another multiplication grid

## Worksheet task: $\mathbf{2 0}$ minutes

This lesson is following on from what your child learned yesterday about multiplying by tens and ones. The purpose of the lesson is to connect what they have learned about patterns in multiplication with patterns for multiplying by decimal numbers.

Tricky part: The difficulty that most children seem to have with decimal numbers is that they want to line up the numbers and decimal points and put decimal points in each line of working. This is irrelevant and confusing. Please instruct your child to ignore the decimal points at the start and just multiply the numbers as if there were no decimal places at all. At the end, work out the number of decimal places needed in the answer. Use the patterns provided to figure out how.

Here are some of the patterns to help:

- $3 \times 5=15$ (no decimal places)
- $0.3 \times 5=1.5$ ( 1 decimal in question $=1$ in the answer)
- $3 \times 0.5=1.5$ ( 1 decimal in question $=1$ in the answer)
- $0.3 \times 0.5=0.15$ ( 2 decimals in question $=2$ in the answer)
- $0.03 \times 5=0.15$ ( 2 decimals in question $=2$ in the answer)
- $0.00003 \times 0.005=0.00000015$ ( 8 decimals in question $=8$ in the answer)

DI2. Decimals in multiplying
TR p92
Multiplying with decimal numbers is very similar to multiplying with whole numbers. Examine the following examples and see if you can find the pattern between the decimals in the terms and the decimals in the answer.

## Example 1:

| 12.4 | $1^{1} 9.3$ | $2^{1} 6.3$ | $2^{1} 4.2$ |
| :---: | :---: | :---: | :---: |
| $\times \quad 2$ | $\times \quad 2$ | $\times 3$ | $\times \quad 4$ |
| 24.8 | 38.6 | 78.9 | 96.8 |

What is the pattern?

Apply this pattern to answer the questions below.
16. 3
$\qquad$
x 2
32. 5

| 17.6 |
| ---: |
| $\times \quad 4$ |

4
15. 3
x 7
$\qquad$
$\qquad$
$\qquad$
$\qquad$

## Example 2:

| 1.24 |
| ---: |
| $\times \quad 2$ |
| 2.48 |

> What is the pattern?

Apply this pattern to answer the following questions:

1. 63
$\qquad$
$\qquad$
2. 73
3. 35
4. 87
$\times \quad 2$ $\qquad$
x $\quad 5$
$\qquad$
$\qquad$

Make up a rule to describe how to know where to put the decimal points when multiplying:

## BACKWARDS QUESTION:

Put the decimal points into the following equation. What other possibilities are there? Write as many as you can:
$124 \times 2=0.248$

D13. Decimals in multiplying 2
Multiplying with decimal numbers is very similar to multiplying with whole numbers. Examine the following examples and see if you can find the pattern between the decimals in the terms and the decimals in the answer.

## Examples:

| 5. 4 | 0.54 | 54 | 54 |
| :---: | :---: | :---: | :---: |
| $\times 2.3$ | X 2.3 | x 2.3 | x 0.23 |
| 162 | 162 | 162 | 162 |
| 1080 | 1080 | 1080 | 1080 |
| 12.42 | 1.242 | 124.2 | 12.42 |

What is the pattern?

Apply this pattern to answer the questions below.

| 56 |  | 57 | 5. 6 | 7.4 |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\times 0.43$ | x | 5.8 | x 0.82 | x | 6. 3 |
|  |  |  |  |  |  |

Check your answers with a calculator. If you are still having difficulty seeing the pattern, go back and look at the examples again. Compare the total number of decimal places in the question with the total number of decimal places in the answer. Show your answers to your teacher before continuing.

Make up a rule to describe how to know where to put the decimal points when multiplying:

## BACKWARDS QUESTION:

Put the decimal points into the following equation. What other possibilities are there? Write as many as you can:
$54 \times 23=1.242$

## Thursday: Interleaved Practice Questions

## Why we are using mixed up questions:

In this lesson your child will be reviewing a range of skills that they have learned previously. Each question is unrelated to the previous question, because we want your child to have to think hard about what to do. Mixing up questions like this, rather than just practising related questions, has been shown in research to improve student retention of concepts by $60 \%$ over a 4 month period.

## What to expect:

Your child will probably have forgotten how to complete quite a few of the questions. If needed, change the numbers in each question to make them easier because this will still require your child to think hard and remember a process. If they still can't work it out, feel free to show them, but try using different numbers rather than the exact same question. There are answers to each question on the website in case you get stuck.

## Interleaved practice

Number:
Number:

1. Add the missing numbers to the number line

2. $523-(147+292)=$

$523-147+292=\square$
What is the same about these equations and what is different?
3. Write the numbers 20 to 35 in the correct box.

| Prime Numbers | Composite Numbers |
| :---: | :---: |
|  |  |

4. Round these numbers to two decimal places:
4.7359
127.903823
15.01494
23.40975
5. Write 5 multiples for these numbers:

15: $\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
32: $\qquad$
$\qquad$
$\qquad$ ____

Measurement/Geometry:
6. The small cubes in this 3 D object are $1 \mathrm{~cm}^{3}$. What is the volume of the whole object?

7. You need to catch a bus to school from Main Road and be there in time for sports practice at 8:30am. Use the timetable to decide when you need to be at your bus stop and why.

| Stops | Central <br> line | Central <br> line | Central <br> line | Central <br> line |
| :--- | :---: | :---: | :---: | :---: |
| Junction Street | $7: 46 \mathrm{am}$ | $8: 01 \mathrm{am}$ | $8: 16 \mathrm{am}$ | $8: 31 \mathrm{am}$ |
| Main Road | $7: 48 \mathrm{am}$ | $8: 03 \mathrm{am}$ | $8: 18 \mathrm{am}$ | $8: 33 \mathrm{am}$ |
| Anzac Avenue | $7: 52 \mathrm{am}$ | $8: 07 \mathrm{am}$ | $8: 22 \mathrm{am}$ | $8: 37 \mathrm{am}$ |
| Central School | $7: 55 \mathrm{am}$ | $8: 10 \mathrm{am}$ | $8: 25 \mathrm{am}$ | $8: 40 \mathrm{am}$ |
| Central Shopping <br> Centre | $8: 01 \mathrm{am}$ | $8: 16$ | $8: 31 \mathrm{am}$ | $8: 46 \mathrm{am}$ |

## Chance/Data:

8. In this graph, each block represents 5 people.

How many people like each colour?
What fraction of the sample (group of people asked) like each of the colours: Blue, Yellow or Purple?

Which two colours together were chosen by $50 \%$ of the sample?


## Friday: Connecting Lesson

## Distributive Law

In the previous lessons this week we have considered multiplying by tens and also multiplying by ones. In this lesson your child will put these ideas together unpack a very important property of multiplication called the distributive law or the distributive property. Given the work that they have done on multiplying by tens and ones on Wednesday, this worksheet should be relatively simple.

Please consider reviewing the Lego poster from earlier this week and checking that your child is remembering those particular number facts more easily.

Here are a few quick grids of the facts that students tend to find the most difficult to recall. Feel free to use them for practice instead. They have fewer calculations, but are the harder ones.

|  | 3 | 4 | 6 | 7 | 8 |
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|  | 3 | 4 | 6 | 7 | 8 |
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|  | 3 | 4 | 6 | 7 | 8 |
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|  | 3 | 4 | 6 | 7 | 8 |
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## D4. Mental partitioning and multiplication

Often using mental strategies when multiplying is quicker than using a calculator. Look at the following example, find the pattern, and use it to solve the problems below.

What you already know... $44 \times 5=(40 \times 5)+(4 \times 5)=200+20=220$
This is called the distributive law. Use it to try the following questions, then extend it to include multiples of ten and decimal numbers in the questions below.

## Try these:

$34 \times 5=$ (
) $=$ $\qquad$ $+$ $\qquad$ $=$ $\qquad$ $62 \times 3=($
) + (
) $=$ $\qquad$ $+$ $\qquad$
$\qquad$

## Extending the distributive law for multiplication:

## Multiples of ten:

| $340 \times 5=($ | $)+($ | $)=\square$ |
| :--- | :--- | :--- |
| $620 \times 30=($ | $)+($ | $=\square$ |
| $304 \times 5=($ | $)$ | $=\square$ |
| $602 \times 30=($ | $)+($ | $=\square$ |

Decimals:

| $3.4 \times 5=($ | $)+($ | $)=$ |
| :--- | :--- | :--- |
| $6.2 \times 3=($ | $)=\square$ |  |

Check your answers with your teacher or with a calculator to make sure that you have found an appropriate process to use before continuing.

What patterns or processes have you found that work for all of the questions above?

What do you think the distributive law does?

## BACKWARDS QUESTIONS:

$6.02 \times 3=$
$3.4 \times \square=1.7$
$\square \times 0.3=1.86$

